

Warm Up

If the $\sin(A) = \frac{5}{13}$, find the following for triangle ABC.

Missing side 12

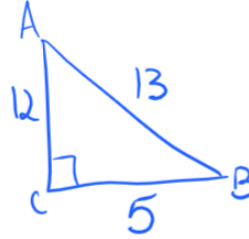
$\cos(A) = \frac{12}{13}$

$\tan(A) = \frac{5}{12}$

$\sin(B) = \frac{12}{13}$

$\cos(B) = \frac{5}{13}$

$\tan(B) = \frac{12}{5}$



Missing side

$$5^2 + b^2 = 13^2$$

$$25 + b^2 = 169$$

$$b^2 = 144$$

$$b = 12$$

Today, we are going to discuss:

Circles

- The equation for a circle on the coordinate plane

- Identifying radius, center and points on a circle.

Geometry in Coordinate Plane

Up until now we have been learning about lines. Match each blue with its corresponding orange.

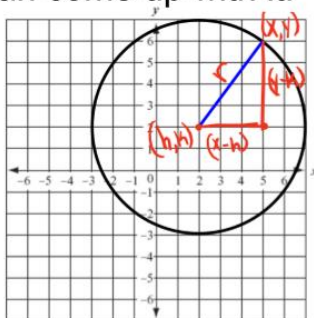
1. $y = mx + b$: $\left(\frac{ax_2 + bx_1}{a+b}, \frac{ay_2 + by_1}{a+b} \right)$
2. parallel : $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$
3. perpendicular : $m = \text{slope}, b = \text{y-intercept}$
4. distance : same slope
5. section formula : opposite reciprocal slope

Now we are going to learn about circles.

Don't forget $y - y_1 = m(x - x_1) \rightarrow$ point slope formula.

Used to find the equation of a line through a given point.

Circles have their own equation. Lets see if we can come up with it.



Use Pythagorean Theorem.

$$(x-h)^2 + (y-k)^2 = r^2$$

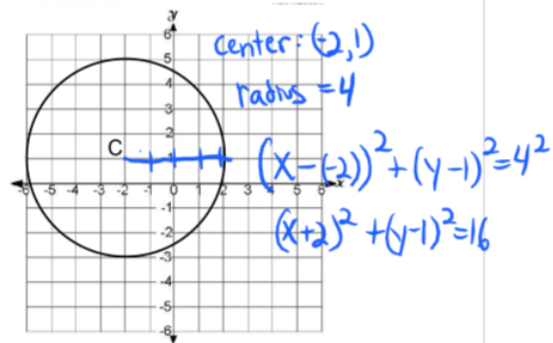
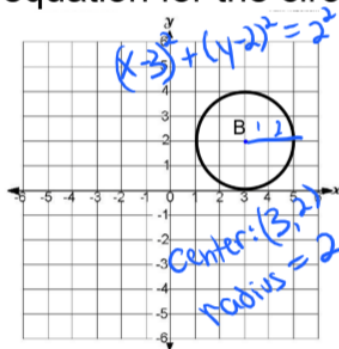
Standard Form Equation

$$(x-h)^2 + (y-k)^2 = r^2$$

(h, k) is the center

r is the radius

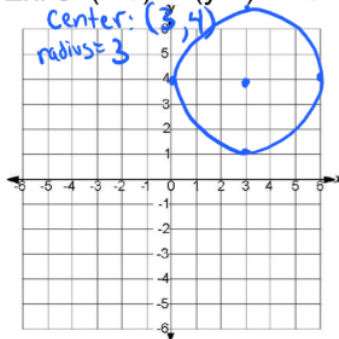
Identify the center and radius, then write an equation for the circle.



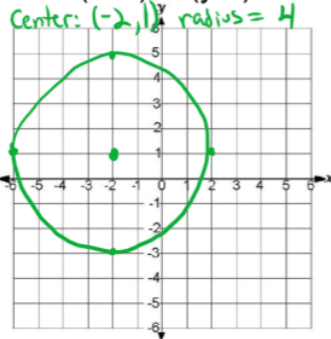
Identify the center and radius of a circle given its equation. Then graph it.

Geometry in Coordinate Plane

Ex. 3 $(x-3)^2 + (y-4)^2 = 3^2$



Ex. 4 $(x+2)^2 + (y-1)^2 = 16$

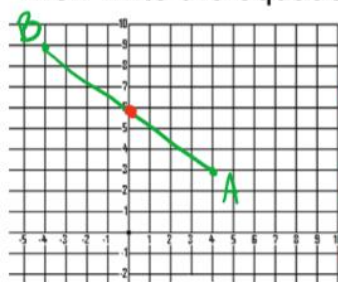


Another way to look at it.

Geometry in Coordinate Plane

Given that the diameter of a circle lies on points A(4,3) and B(-4,9); Identify the center and length of the radius.

Then write the equation of the circle.



Find Center
 $(x, y) = \left(\frac{4 + (-4)}{2}, \frac{3 + 9}{2} \right)$
 $(x, y) = \left(\frac{0}{2}, \frac{12}{2} \right)$
 $(x, y) = (0, 6)$

use midpoint formula.

Find length of radius

Find distance of diameter divide in half for radius.

$AB = \sqrt{(4 - (-4))^2 + (3 - 9)^2}$

$AB = \sqrt{(8)^2 + (-6)^2}$

$AB = \sqrt{64 + 36}$

$AB = \sqrt{100} = 10$

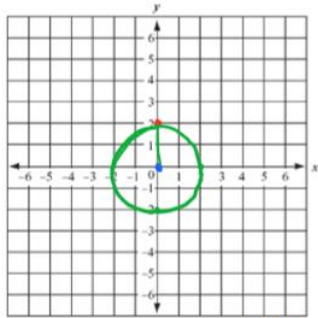
so $r = 5$

Equation: $(x-0)^2 + (y-6)^2 = 5^2$
 $(x)^2 + (y-6)^2 = 25$

One more type of problem

Geometry in Coordinate Plane

Prove or disprove that the point $(1, \sqrt{3})$ lies on a circle centered at the origin and containing the point $(0, 2)$.



Algebraically, it is shown that point $(1, \sqrt{3})$ lies on the given circle with equation $x^2 + y^2 = 4$.

Does point $(1, \sqrt{3})$ lie on the circle? If so, it will make the circle equation true.

Equation of circle.

center: $(0, 0)$

radius: 2

$$(x-0)^2 + (y-0)^2 = 2^2$$

$$x^2 + y^2 = 4$$

Check point

$(1, \sqrt{3})$

(x, y)

$$x^2 + y^2 = 4$$

$$(1)^2 + (\sqrt{3})^2 = 4$$

$$1 + 3 = 4$$

$$4 = 4 \checkmark$$

You do one

Geometry in Coordinate Plane

Prove or disprove that point $(8, 4)$ lies on a circle that is centered at $(2, -4)$ and contains the point $(10, -10)$.

Equation of Circle

Center: $(2, -4)$

radius: Distance from center to point on circle

$$r = \sqrt{(10-2)^2 + (-10-(-4))^2}$$

$$r = \sqrt{8^2 + (-6)^2}$$

$$r = \sqrt{64 + 36}$$

$$r = \sqrt{100} = 10$$

Equation

$$(x-2)^2 + (y-(-4))^2 = 10^2$$

$$(x-2)^2 + (y+4)^2 = 100$$

Recap:

What is the standard form equation of a circle?

$$(x-h)^2 + (y-k)^2 = r^2$$

Given the two points that make a diameter of a circle, how would you find the coordinates for the center? Use midpoint formula

Check given point

$$(x-2)^2 + (y+4)^2 = 100$$

$(x, y) = (8, 4)$

$$(8-2)^2 + (4+4)^2 = 100$$

$$6^2 + 8^2 = 100$$

$$36 + 64 = 100$$

$$100 = 100 \checkmark$$

The above work shows point $(8, 4)$ lies on the given circle.